



# Lecture 9

## Transient Laser Behavior\*

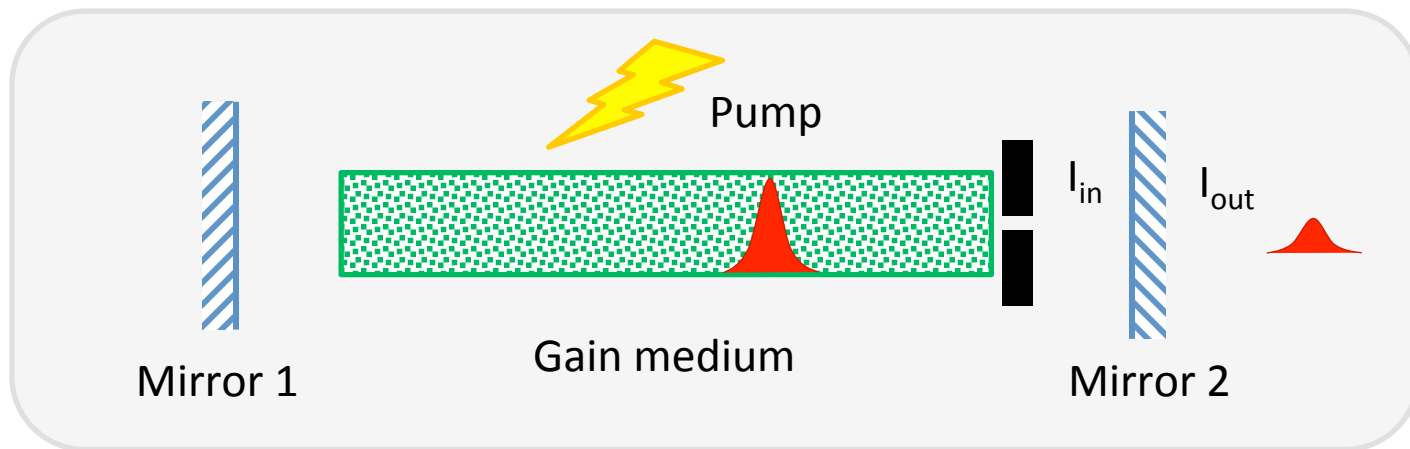
Min Yan

Optics and Photonics, KTH

# Reading

- *Principles of Lasers* (5th Ed.): Chapter 8.
- Skip: 8.4.4, 8.6.4.
- Squeeze: 8.2.1.

# Laser



- $R_p$  and  $\gamma$  are a function of time
  - An inherent property of lasers (as a nonlinear system)
  - Purposely introduced (via pump and loss modulation)

# Contents

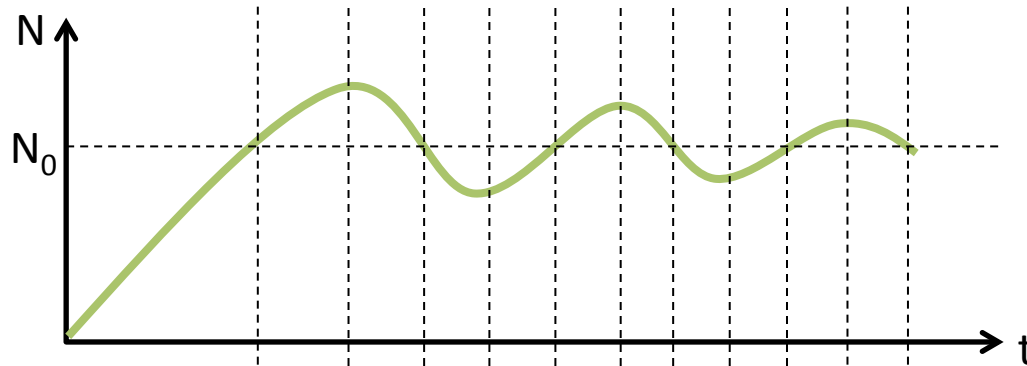
Content	Time
1. Relaxation oscillation	5'
2. Q-switching	30'
3. Gain-switching	5'
4. Mode-locking	35'
5. Cavity-dumping	5'
Total:	80'

# Contents

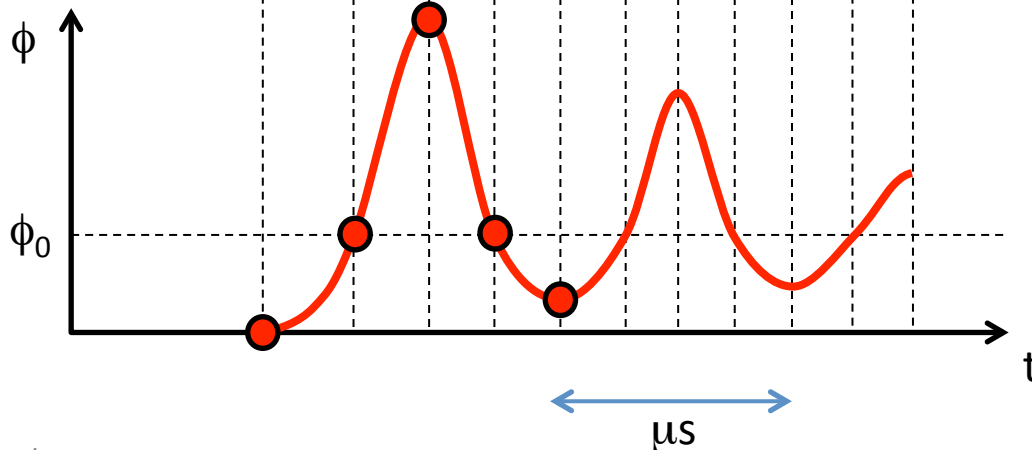
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# Relaxation oscillation

- 4-level case
- Single-mode



- Laser spikes
- Periodic after  $\sim 10$  oscillations
- $N$  leading by  $T/4$
- $N \propto \exp(-t/t_0)\cos(\omega t + \beta)$
- $\phi \propto \exp(-t/t_0)\sin(\omega t + \beta)$



If  $\frac{1}{t_0} < \omega$

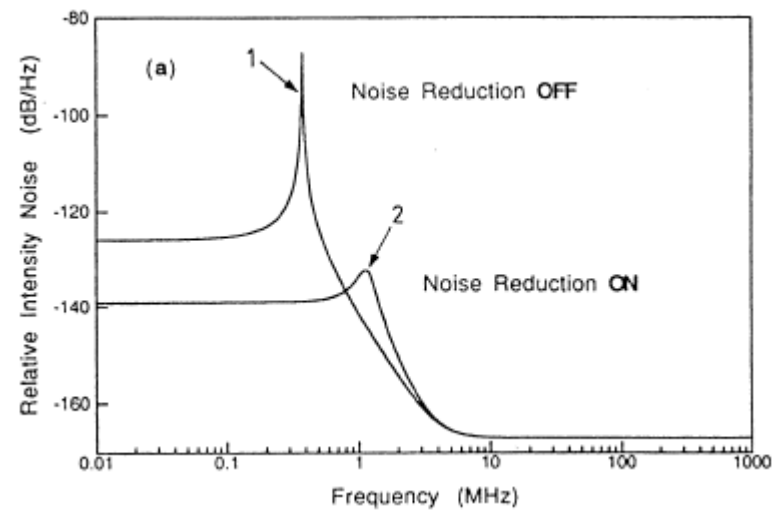
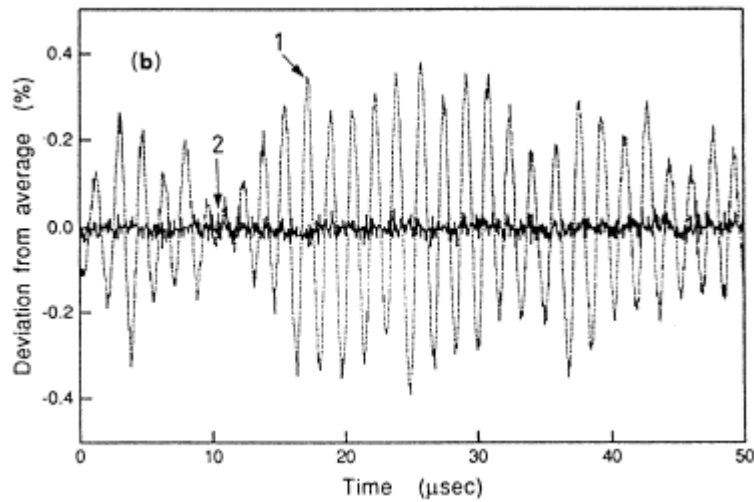
$$t_0 = \frac{2\tau}{x}$$

$$\omega \approx \sqrt{\frac{x-1}{\tau_c\tau}}$$

where  $x = \frac{R_p}{R_{cp}}$

# Pulsation

Nd:YAG



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# Q-switching: Principle

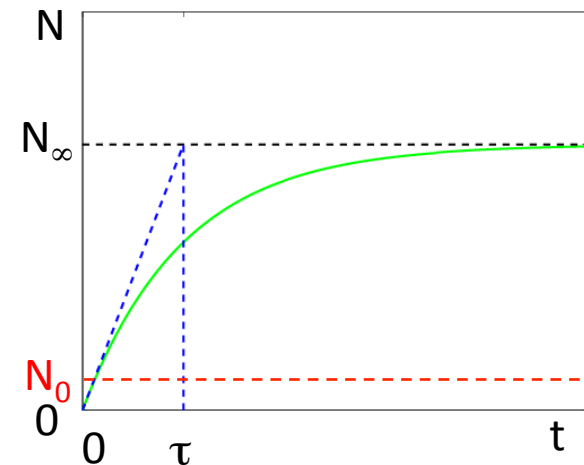
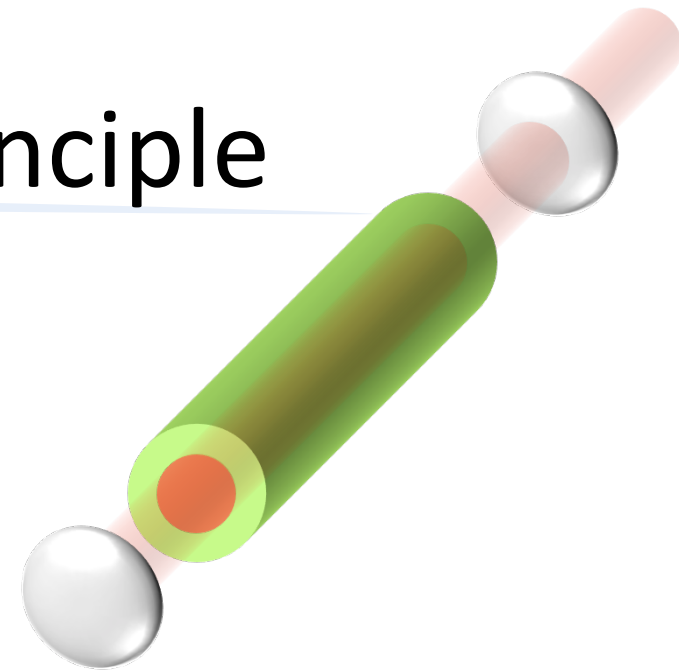
- **CW laser:**  $N_0=N_c$
- **Q-switched laser (4L)**

$$\frac{dN}{dt} = R_p - B\phi N - \frac{N}{\tau}$$

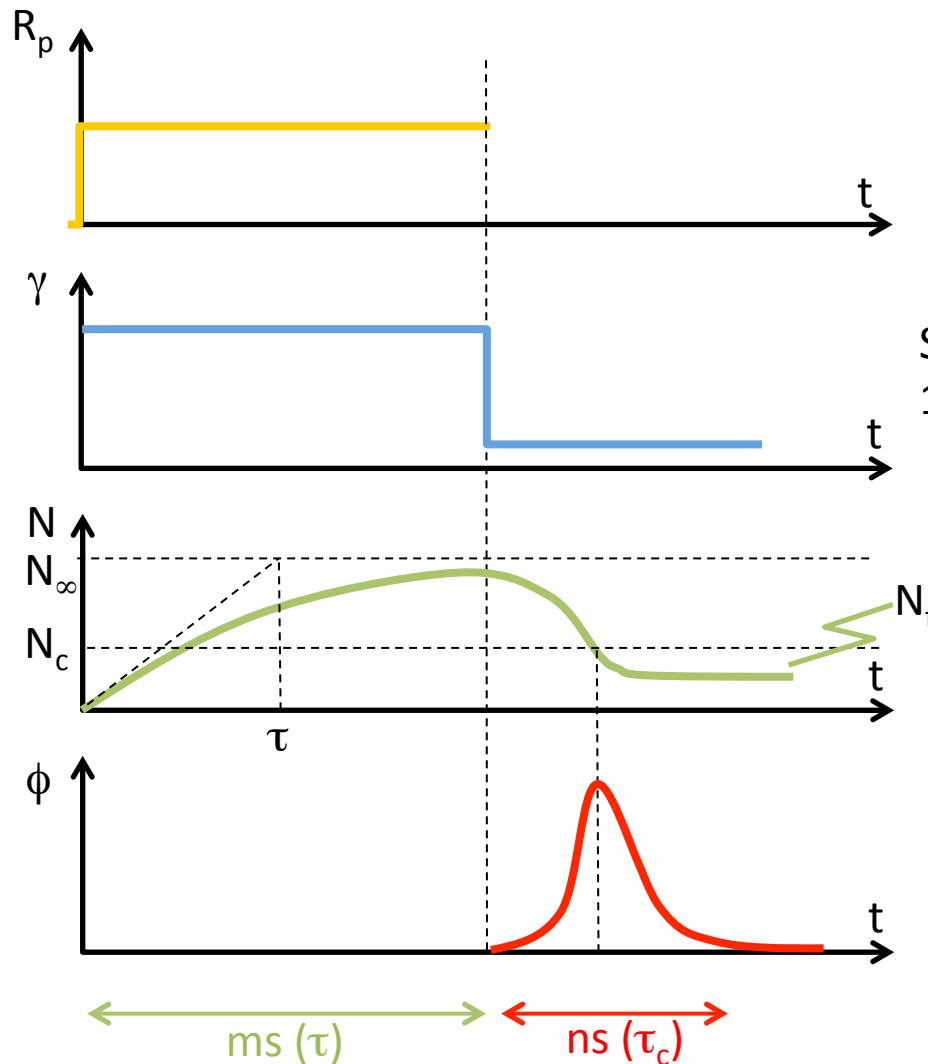
Let  $\phi=0$ , 
$$\frac{dN}{dt} = R_p - \frac{N}{\tau}$$

One has 
$$N(t) = N_\infty \left[ 1 - \exp\left(-\frac{t}{\tau}\right) \right]$$
  
with  $N_\infty = R_p\tau$

- Longer  $\tau$  (ms) preferred (larger  $N_\infty$ )
- Pump duration  $< \tau$
- Lasers applicable: most solid-state lasers (Nd, Yb, Eb, Ho based) and some gas lasers ( $\text{CO}_2$ , iodine)



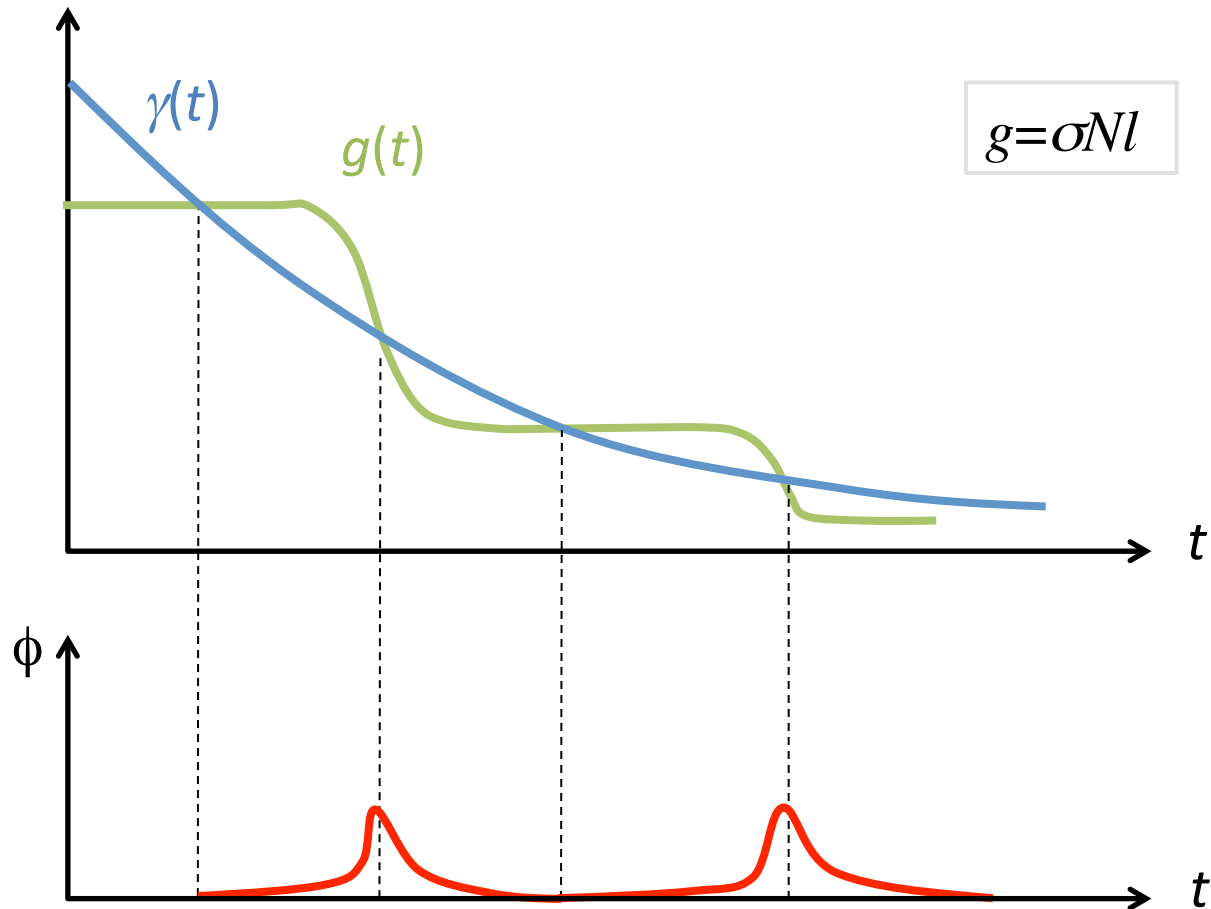
# Q-switching: Fast



Switching time:  
10 ps ~ 100 ns

Pulse spatial width:  
 $\Delta z_p = 2ns \cdot c = 0.6m$

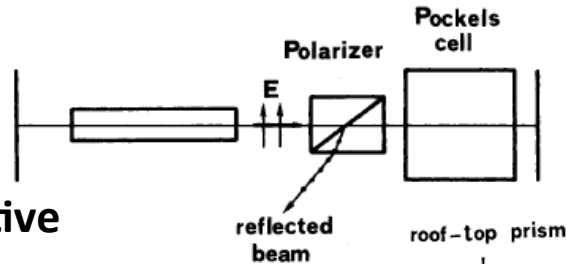
# Q-switching: Slow



# Q-switching: Methods

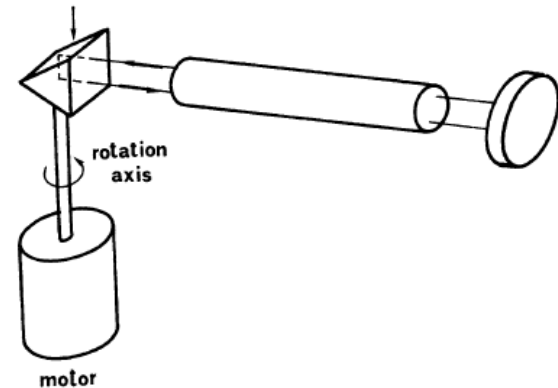
- **Electro-optical**

- Most common **active**
- Fast ( $t_s < 20\text{ns}$ )
- High voltage (up to 5kV)



- **Rotating mirror**

- Simple, inexpensive, any wavelength
- Noisy, slow ( $t_s = 400\text{ns}$  for 400rps)

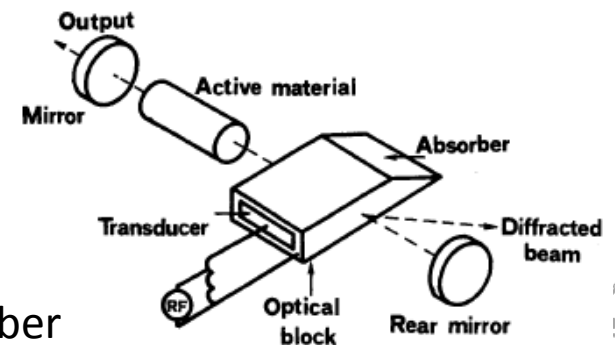


- **Acousto-optic**

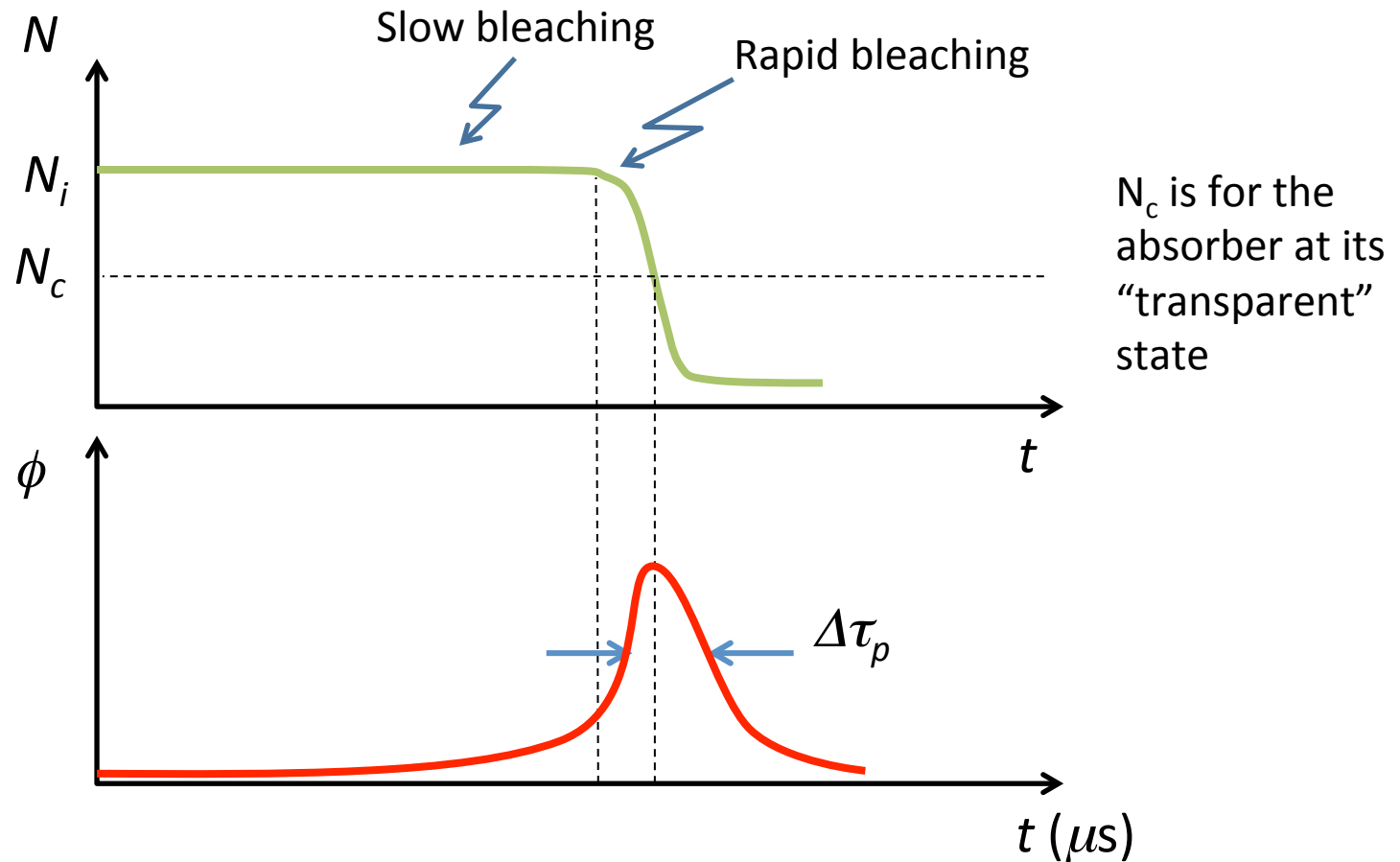
- Low insertion loss, high repetition (kHz)
- Slow (due to acoustic wave propagation)

- **Saturable-absorber**

- Most common **passive**
- Favor **single-mode**
- Photochemical degradation of (dye) absorber
- (Hence) low average power lasers



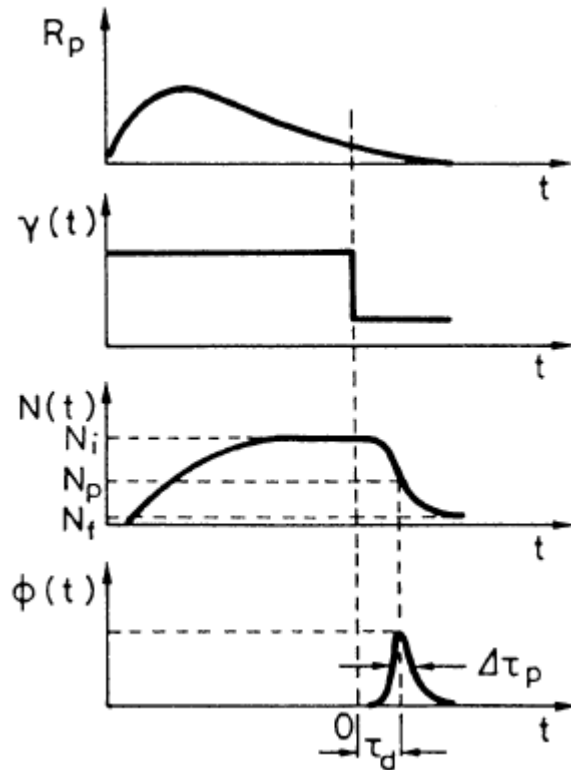
# Saturable-absorber Q-Switching



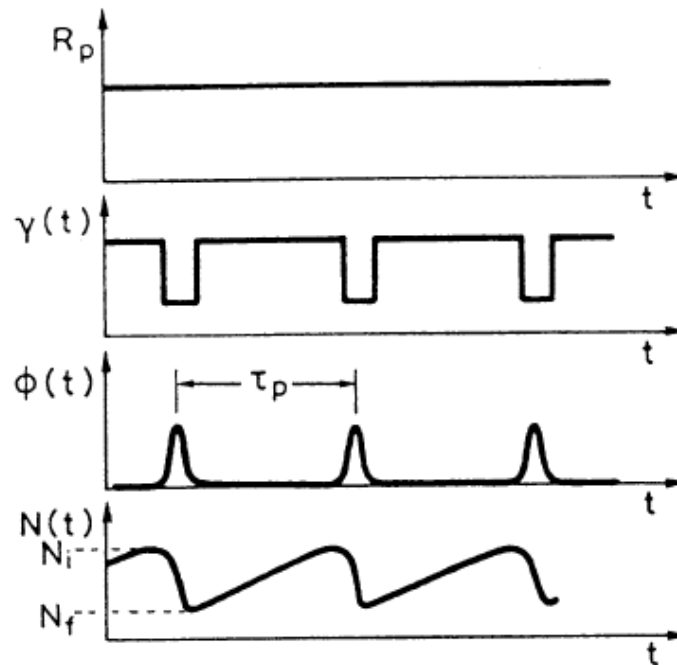
**Slow bleaching ( $\mu\text{s}$ ):** promotes the mode with lowest loss/highest gain

# Operation schemes

- **Pulsed** ( $R_p$ ) ( $<100\text{Hz}$ )
- Electro-optical or mechanical shutters



- **Continuously pumped** Repetitively Q-switched ( $\text{kHz} \sim <100\text{kHz}$ , low gain)
- Acousto-optic, mechanical, saturable absorber shutters

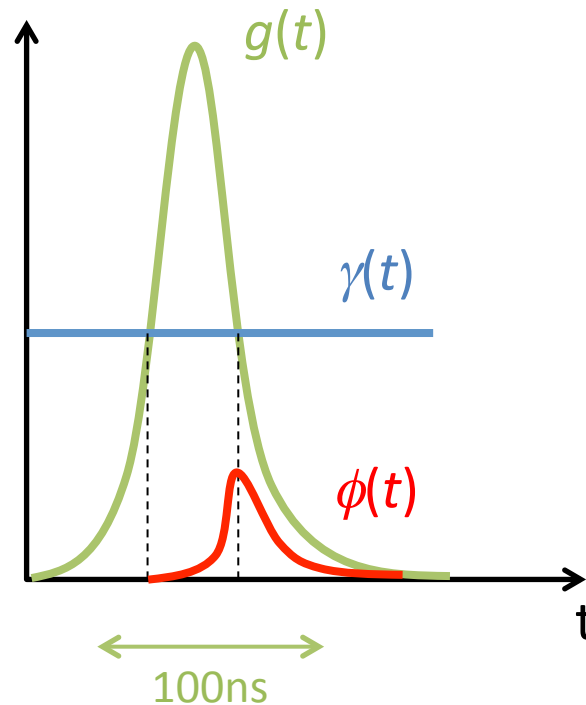


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# Gain switching

- **Q switching:** Loss  $\downarrow$  rapidly
- **Gain switching:** gain  $\uparrow$  rapidly
  - Pump duration 5-20  $\tau_c$  ( $<1\mu\text{s}$ )
  - Rp peak: 4-10 times  $R_{cp}$
  - Laser spiking



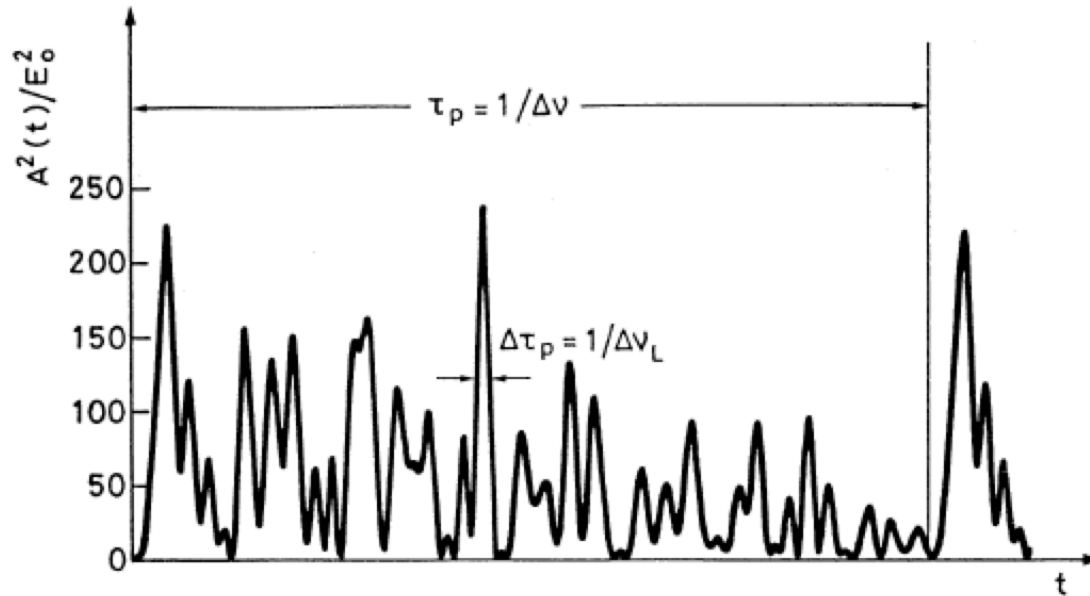


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# Before mode-locking

- **CW laser with multiple longitudinal modes:**  
phases among modes are random  $\rightarrow$  approx. constant output



$$E(t) = \sum_{l=0}^{30} E_0 \exp\{j [(\omega_0 + l\Delta\omega)t + \varphi_l]\}$$

# Mode-locking: Principle

- **Mode-locked:** Phases are correlated → pulsed output

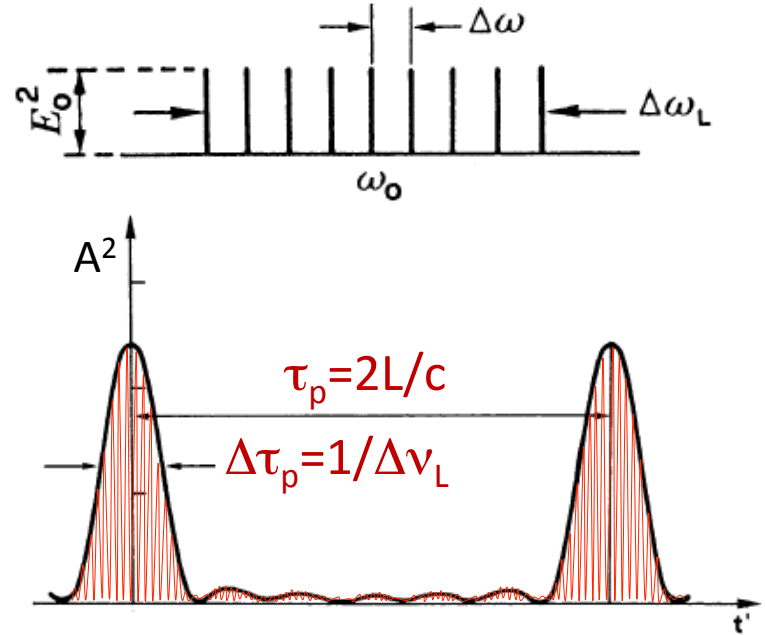
Equal-amplitude case:

Let  $\varphi_l - \varphi_{l-1} = \varphi$

$$\begin{aligned}
 E(t) &= \sum_{l=-n}^n E_0 \exp\{j[(\omega_0 + l\Delta\omega)t + l\varphi]\} \\
 &= \sum_{l=-n}^n E_0 \exp[jl(\Delta\omega t + \varphi)] \exp(j\omega_0 t) \\
 &= A(t) \exp(j\omega_0 t)
 \end{aligned}$$

Let  $t' = t + \varphi/\Delta\omega$

$$\begin{aligned}
 A(t') &= \sum_{l=-n}^n E_0 \exp(jl\Delta\omega t') \\
 &= E_0 \frac{\sin\left[\frac{(2n+1)\Delta\omega t'}{2}\right]}{\sin\left(\frac{\Delta\omega t'}{2}\right)}
 \end{aligned}$$



- **Max**  $\frac{\Delta\omega t'}{2} = m\pi \rightarrow t' = m \frac{2\pi}{\Delta\omega} = m \frac{1}{\Delta\nu} = m \frac{2L}{c}$   
 $E_{\max}^2 = (2n + 1)^2 E_0^2$
- **Min**  $t' = \frac{2\pi}{(2n+1)\Delta\omega} = \frac{1}{\Delta\nu_L}$

(m=0, pulse width)

# Mode-locking: Pulse width

Gaussian gain profile

$$\Delta\tau_p = \frac{0.441}{\Delta\nu_L}$$



In general a **transform-limited pulse** has:  $\Delta\tau_p = \frac{\beta}{\Delta\nu_L}$  with  $\beta \approx 1$

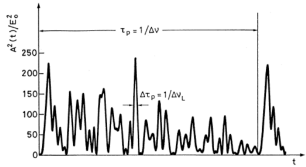
- **Inhomogeneously** broadened gain medium ( $\gg$  threshold):  $\Delta\tau_p \approx \frac{0.441}{\Delta\nu_0}$
- **Homogeneously** broadened gain medium:  $\Delta\tau_p \approx \frac{0.45}{\sqrt{\Delta\nu \Delta\nu_0}}$

## Example:

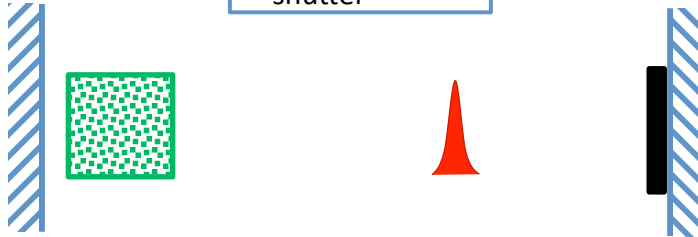
If  $\Delta\nu_0 = 200\text{GHz} \rightarrow \Delta\tau_p \approx 2\text{ps} \rightarrow \Delta z_p = \Delta\tau_p \cdot c \approx 0.6\text{mm}$

If  $\Delta\nu_0 = 2\text{THz} \rightarrow \Delta\tau_p \approx 200\text{fs} \rightarrow \Delta z_p = \Delta\tau_p \cdot c \approx 0.06\text{mm}$

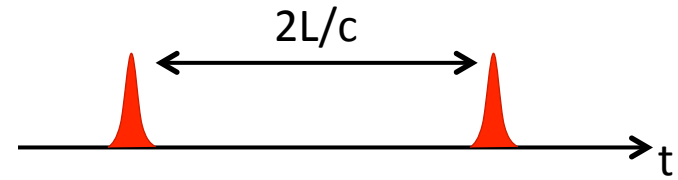
# Mode-locking: Implementation



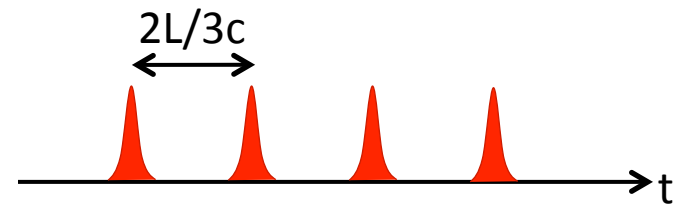
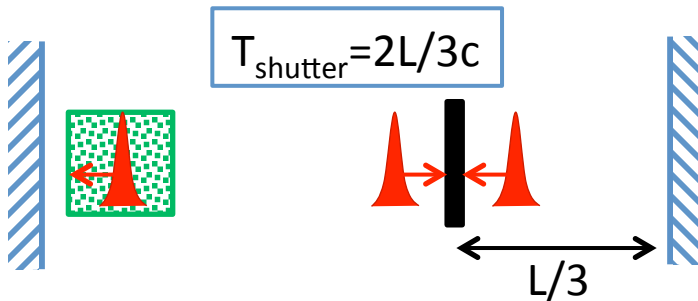
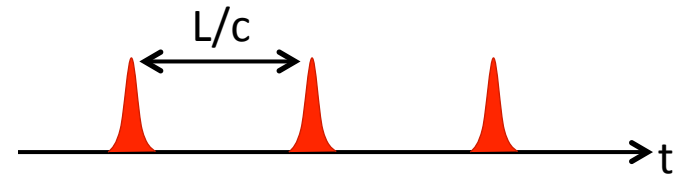
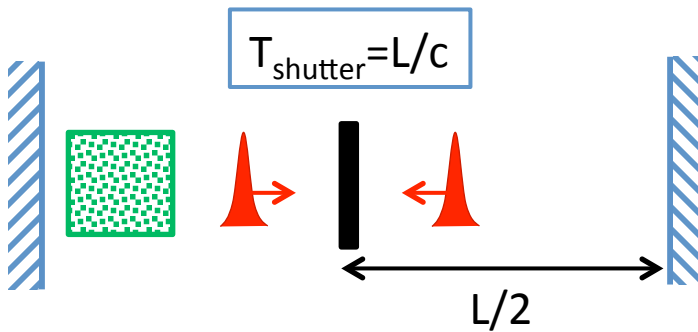
Fundamental



Phase locking  $\equiv$  discrimination in time



Harmonic



# Mode-locking: Methods

- **Active**

- Amplitude-modulation (AM)

- ❖ Principle: change  $\gamma$  ( $\omega_m = 2\pi\Delta\nu$ )

- ❖ Approach: Pockels cell, or acousto-optic modulator

- Phase-modulation (FM) [less used]

- ❖ Principle: change  $L_e$  (oscillating mirror)

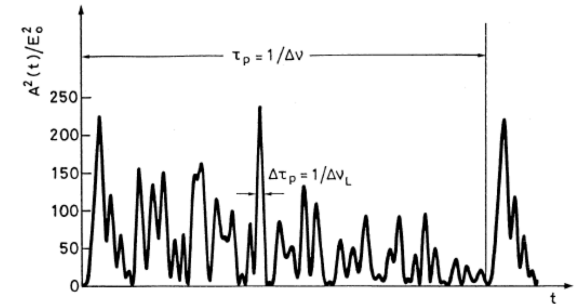
- ❖ Approach: Pockels cell

- Synchronous-pumping [less used]

- **Passive**

- Fast\* saturable absorber [10s of ps, strongest survives]

- Kerr lens [ $n = n_0 + n_2 I$ , self-focusing, **instantaneous response**]



\* **Absorber** is FAST if its relaxation time is comparable to a ML pulse duration.

\* **Gain medium** is FAST if its lifetime is comparable to cavity round-trip time.

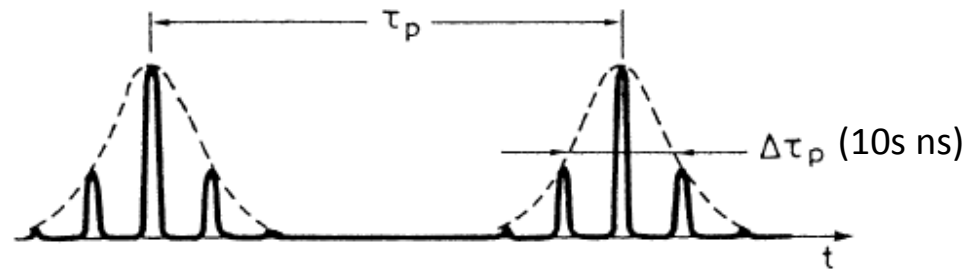
# Mode-locking: Pumping schemes

- **Continuous pump**

- Active/passive ML
- Passive ML: Q-switching can emerge (slow gain medium)



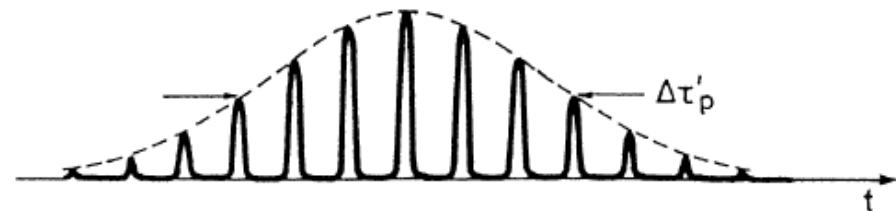
Fast shutter + fast gain medium



Fast saturable absorber + slow gain medium (100s  $\mu$ s)  
(Repetitive Q-switching + ML)

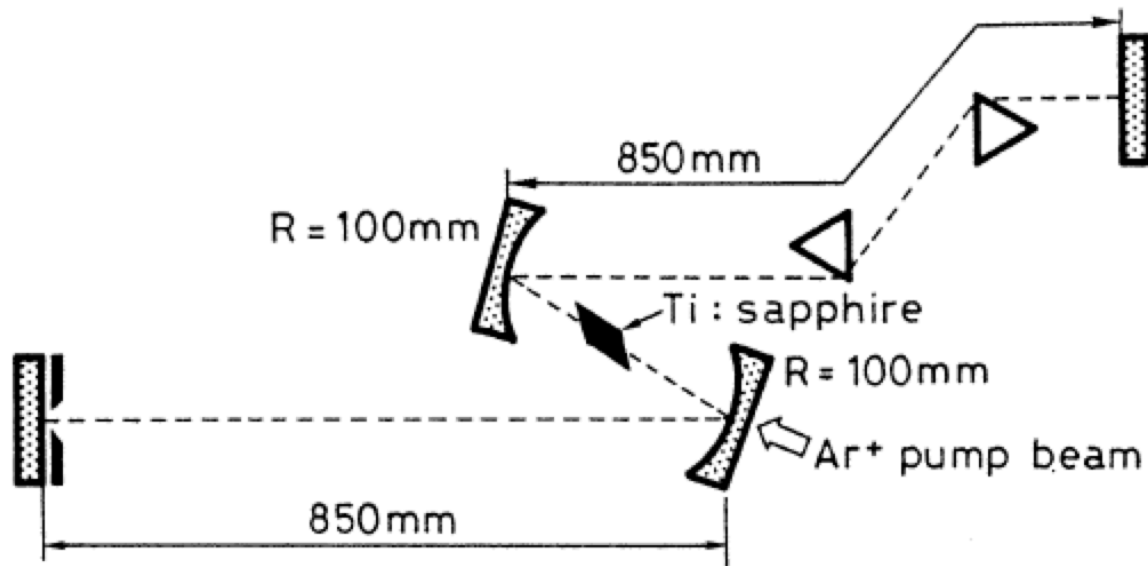
- **Pulsed pump**

- Active/passive ML
- Passive ML:  $\Delta\tau_p'$  can be pump time or due to Q-switching



# Ti:Sapphire Laser

Laser medium	$\Delta\nu_0$	$\sigma[10^{-20} \text{ cm}^2]$	$\tau[\mu\text{s}]$	$\Delta\tau_p$	$\Delta\tau_{mp}$
Ti:sapphire	100 THz	38	3.9	6–8 fs	4.4 fs



Ti:Sapphire plate: 10mm thick

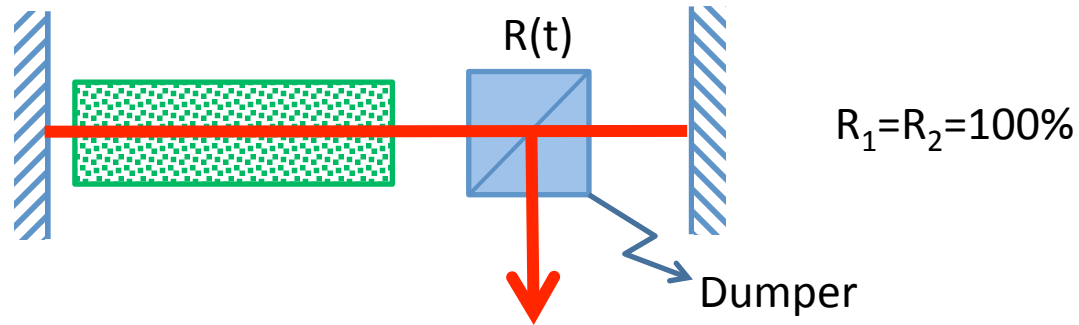


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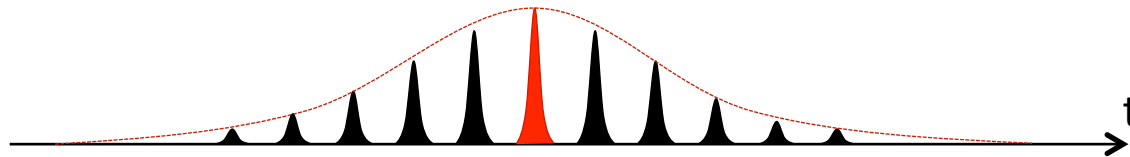
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# Cavity dumping

Applicable to CW, **mode-locked**, and Q-switched lasers.



- **Pulsed-pump ML:** dump pulse with highest intensity [Pockels cell]



- **CW-pump ML:** dump a train of laser pulses of lower repetition rate (100k~1MHz) & higher peak power [Acousto-optic grating]

